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F O R S C H U N G S P R A X I S  
for  
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## **Incremental Learning of Stable Dynamical Systems using Diffeomorphic Transformations**

### Problem description:

Recent work in Programming by Demonstration suggests to encode robotic skills into stable dynamical systems (DS). DS have been proven to be flexible enough to accurately represent complicated motions [1]–[4]. Moreover, robots driven by stable DS are guaranteed to reach the desired position, and can react in real-time to external perturbations. Stable DS systems are usually learned off-line by solving a constrained optimization problem [1, 3]. Alternative approaches [2, 4] are fast enough to work online, but they require an initial DS with a fixed structure.

In this Forschungspraxis work, the student has to implement an incremental learning algorithm to allow the on-line refinement of a diffeomorphic transformation. The learned diffeomorphism will transform the trajectories of a generic stable DS to match the demonstrated movements. To permit incremental learning, the diffeomorphism will be represented using an extreme learning machine (ELM) [5], and on-line least square approaches will be used to train the ELM's parameters. The developed approach will be compared with state-of-the-art approaches [1, 4] in terms of training time and accuracy.

### Work schedule:

- Literature research on motion representation with dynamical systems
- Implement an incremental learning approach to refine a diffeomorphic transformation
- Comparison with state-of-the-art approaches [1, 4]

### Bibliography:

- [1] S. M. Khansari-Zadeh and A. Billard, “Learning control lyapunov function to ensure stability of dynamical system-based robot reaching motions”, in *RAS*, vol. 62, n. 6, pp. 752–765, 2014.
- [2] C. Blocher, M. Saveriano, and D. Lee, “Learning Stable Dynamical Systems using Contraction Theory”, in *URAI*, pp. 124–129, 2017.
- [3] K. Neumann and J. J. Steil, “Learning robot motions with stable dynamical systems under diffeomorphic transformations”, in *RAS*, vol. 70, pp. 1–15, 2015.
- [4] N. Perrin and P. Schlehüser-Caissier, “Fast diffeomorphic matching to learn globally asymptotically stable nonlinear dynamical systems”, in *Systems & Control Letters*, vol. 96, pp. 51–59, 2016.
- [5] G.-B. Huang, Q.-Y. Zhu, and C.-K. Siew, “Extreme learning machine: theory and applications”, in *Neurocomputing*, vol. 70, n. 1, pp. 489–501, 2006.

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